Test #2	AMATYC Student	Mathematics League	February/March 2004
1. A stock loses 60% of its v A. 60% B. 120%	alue. What must the C. 150%	percent of increase be t D. 200% E. 30	to recover all of its lost value? 00%
2. Which of the following is NOT a factor of $x^4 - 4x^3 - x^2 + 16x - 12$?			
A. x - 2 B. x + 2	C. x - 1	D. x + 1	E. x - 3
3. The library in Johnson C biographies, and 1/17 are atA. 240 B. 250	ity has between 1000 lases. How many boo C. 270) and 2000 books. Of the oks are either biographi D. 280 E. 30	ese, 25% are fiction, 1/13 are es or atlases? 0
4. A tricimal is like a decim For example, 16/27 = 1/3 + 2/	al, except the digits i 9 + 1/27 = 0.121 as a tr	represent fractions with icimal. How is 77/81 ex	powers of 3 instead of 10. pressed as a tricimal?
5. The function $P(t) = \cos \theta t$	can be written as su	ms and differences of n	L, 0.2212
written that way, what is th	e coefficient of (cos t) ³ ?	
A. 0 B. 1	C1 [D. 2 E2	
6. If $\log_a b = 64$, find $\log_{a^2} A$. 16 B. 48	o ³ . C. 128/3 [D. 96 E. 512	
7. The number 877530p765q6 is divisible by both 8 and 11, with p and q both digits from 0 to 9. The number is also divisible by			
A. 7 B. 12	C. 16 D. 18	E. not enough	information to know
8. Teams A and B play a series of games; whoever wins two games first wins the series. If Team A has a 70% chance of winning any single game, what is the probability that Team A wins the series?			
A. 0.616 B. 0.637	C. 0.657 D	D. 0.700 E. 0.784	ļ
9. The Venn diagram at the A, B and C (not necessarily pending on how the diagram many different answers are number of elements in the A - B is all elements which	e right represents set in that order). De- m is labeled, how possible for the set A - B ? (Note: are in A but not in B)	S 4 0	
A. 2 B. 3 C. 4	D. 5 E. 6		2
10. A fixed point for a function $y = f(x)$ is a real number r such that $f(r) = r$. How many of the following functions must have a fixed point?			
polynomial function of odc trigonometric function y = A	degree > 1 A sin Bx + D	polynomial function of rational function y = (x	f even degree > 0 - a)/(x - b)
A. 0 B. 1 (C. 2 D. 3	E. 4	

11. Which of the following is the identity function f(x) = x for all real numbers?

E. $\sqrt{x^2}$ A. e^{ln x} B. In e^x C. sin(arcsin x) D. arctan(tan x)

February/March 2004 AMATYC Student Mathematics League

12. A circular table is pushed into a corner of a rectangular room so that it touches both walls. A point on the edge of the table between the two points of contact is 2 inches from one wall and 9 inches from the other wall. What is the radius of the table?

A. 5 inches B. 12 inches C. 15 inches D. 17 inches E. 20 inches

13. In $\triangle ABC$, $\angle C = 90^{\circ}$ and $\cos \angle A = 4/5$. If D is the midpoint of side AC, find $\cos \angle CDB$.

A. $\frac{2\sqrt{13}}{13}$ B. $\frac{5}{9}$ C. $\frac{\sqrt{5}}{4}$ D. $\frac{2}{5}$ E. $\frac{3}{5}$

14. Enrique walks along a level road and then up a hill. At the top he immediately turns and walks back to his starting point. He walks 4 mph on level ground, 3 mph uphill, and 6 mph downhill. If the entire walk takes 6 hours, how far does he walk?

A. 16 miB. 20 miC. 24 miD. 28 miE. 32 mi15. If $x^2 = x + 3$, then $x^3 =$ A. x + 6B. 4x + 3C. $4x^2 + 3$ D. $x^2 + 3x + 3$ E. $x^2 + 27$

16. A bag holds 5 cards identical except for color. Two are red on both sides, two are black on both sides, and one is red on one side and black on the other. If you pick a card at random and see that the only side you can see is red, what is the probability that the other side is also red?

A. 1/2 B. 2/3 C. 3/4 D. 4/5 E. 5/6

17. The set S contains the number 2, and if it contains the number n, it also contains 3n and n + 5 (assume S contains only numbers produced by these rules). Which of the following is NOT in S?

A. 2000 B. 2001 C. 2002 D. 2003 E. 2004

18. Let f(x) = ax + b, with b < a both positive integers. If for positive integers p and q, f(p) = 18 and f(q) = 39, what is the value of b?

A. 1 B. 3 C. 4 D. 7 E. 8

19. In \triangle SBC, SB = 12, BC = 15, and SC = 18. Let O be the point for which BO bisects angle SBC and CO bisects angle SCB. If M and L are on sides SB and SC respectively so that ML is parallel to side BC and contains point O, what is the perimeter of \triangle SML?

A. 24 B. 27 C. 30 D. 32 E. 36

20. Ed has four children, AI, Bo, Cy, and Di (in order oldest to youngest). Bo is 4 years older than Cy and 12 years older than Di. This year Ed notices that he is twice as old as Bo, and the sum of the squares of the children's ages equals the square of Ed's age. If Di just became a math teacher, what is the sum of the children's ages?

A. 48 B. 76 C. 100 D. 128 E. 148