## Test #2

## **AMATYC Student Mathematics League**

1. A stock loses 60% of its value. What must the percent of increase be to recover all of its lost value?

A. 60% B. 120% C. 150% D. 200% E. 300%

2. Which of the following is NOT a factor of  $x^4 - 4x^3 - x^2 + 16x - 12$ ?

A. x-2 B. x+2 C. x-1 D. x+1 E. x-3

3. The library in Johnson City has between 1000 and 2000 books. Of these, 25% are fiction, 1/13 are biographies, and 1/17 are atlases. How many books are either biographies or atlases?

A. 240 B. 250 C. 270 D. 280 E. 300

4. A tricimal is like a decimal, except the digits represent fractions with powers of 3 instead of 10. For example, 16/27 = 1/3 + 2/9 + 1/27 = 0.121 as a tricimal. How is 77/81 expressed as a tricimal?

A. 0.950617 B. 0.2012 C. 0.1211 D. 0.1111 E. 0.2212

5. The function  $P(t) = \cos 8t$  can be written as sums and differences of powers of cos t. When P(t) is written that way, what is the coefficient of  $(\cos t)^3$ ?

A. 0 B. 1 C. -1 D. 2 E. -2

6. If  $\log_{a} b = 64$ , find  $\log_{a^2} b^3$ .

A. 16 B. 48 C. 128/3 D. 96 E. 512

7. The number 877530p765q6 is divisible by both 8 and 11, with p and q both digits from 0 to 9. The number is also divisible by

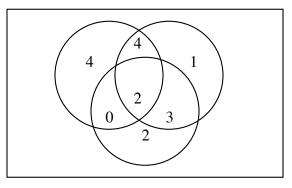
A. 7 B. 12 C. 16 D. 18 E. not enough information to know

8. Teams A and B play a series of games; whoever wins two games first wins the series. If Team A has a 70% chance of winning any single game, what is the probability that Team A wins the series?

A. 0.616 B. 0.637 C. 0.657 D. 0.700 E. 0.784

9. The Venn diagram at the right represents sets A, B and C (not necessarily in that order). Depending on how the diagram is labeled, how many different answers are possible for the number of elements in the set A - B? (Note: A - B is all elements which are in A but not in B)

A. 2 B. 3 C. 4 D. 5 E. 6



10. A fixed point for a function y = f(x) is a real number r such that f(r) = r. How many of the following functions must have a fixed point?

polynomial function of odd degree > 1trigonometric function y = A sin Bx + D polynomial function of even degree > 0 rational function y = (x - a)/(x - b)

A. 0 B. 1 C. 2 D. 3 E. 4

11. Which of the following is the identity function f(x) = x for all real numbers?

A.  $e^{\ln x}$  B.  $\ln e^x$  C.  $\sin(\arcsin x)$  D.  $\arctan(\tan x)$  E.  $\sqrt{x^2}$ 

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12. A circular table is pushed into a corner of a rectangular room so that it touches both walls. A point on the edge of the table between the two points of contact is 2 inches from one wall and 9 inches from the other wall. What is the radius of the table?

B. 12 inches C. 15 inches D. 17 inches E. 20 inches A. 5 inches 13. In  $\triangle ABC$ ,  $\angle C = 90^{\circ}$  and  $\cos \angle A = 4/5$ . If D is the midpoint of side AC, find  $\cos \angle CDB$ . C.  $\frac{\sqrt{5}}{4}$  D.  $\frac{2}{5}$ 2√13 B.  $\frac{5}{9}$ E. A. 14. Enrique walks along a level road and then up a hill. At the top he immediately turns and walks back to his starting point. He walks 4 mph on level ground, 3 mph uphill, and 6 mph downhill. If the entire walk takes 6 hours, how far does he walk? A. 16 mi B. 20 mi C. 24 mi D. 28 mi E. 32 mi 15. If  $x^2 = x + 3$ , then  $x^3 =$ C.  $4x^2 + 3$ D.  $x^2 + 3x + 3$ E.  $x^2 + 27$ B. 4x + 3A. x + 616. A bag holds 5 cards identical except for color. Two are red on both sides, two are black on both sides, and one is red on one side and black on the other. If you pick a card at random and see that the only side you can see is red, what is the probability that the other side is also red? C. 3/4D. 4/5E. A. 1/2B. 2/35/617. The set S contains the number 2, and if it contains the number n, it also contains 3n and n + 5 (assume S contains only numbers produced by these rules). Which of the following is NOT in S? 2000 Β. 2001 C. 2002 D. 2003 2004 A. E. Let f(x) = ax + b, with b < a both positive integers. If for positive integers p and q, f(p) = 18 and 18. f(q) = 39, what is the value of b? C. 3 4 D. 7 E. 8 A. 1 B. 19. In  $\triangle$ SBC, SB = 12, BC = 15, and SC = 18. Let O be the point for which BO bisects angle SBC and CO bisects angle SCB. If M and L are on sides SB and SC respectively so that ML is parallel to side BC and contains point O, what is the perimeter of  $\Delta$ SML? A. 24 B. 27 C. 30 D. 32 E. 36 20. Ed has four children, Al, Bo, Cy, and Di (in order oldest to youngest). Bo is 4 years older than Cy

and 12 years older than Di. This year Ed notices that he is twice as old as Bo, and the sum of the squares of the children's ages equals the square of Ed's age. If Di just became a math teacher, what is the sum of the children's ages?

A. 48 B. 76 C. 100 D. 128 E. 148

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AMATYC STUDENT MATHEMATICS LEAGUE

NAME	KEY Feb/Mar 2004	
	Student's Responses	Local Corrector
1	С	
2	D	
3	Α	
4	E	
5	Α	
6	D	
7	В	
8	E	
9	С	
10	С	
11	В	
12	D	
13	Α	
14	С	
15	В	
16	D	
17	Α	
18	С	
19	С	
20	E	

COLLEGE:		
ROUND: 1 2		
# correct =		
# incorrect =		
# blank=		
$= \# \text{ correct } \times 2$		
$- \qquad = \# \text{ incorrect } \times \frac{1}{2}$		
= score		